

LESSON
13-1

Reteach
Complex Numbers and Roots

An **imaginary number** is the square root of a negative number.

Use the definition $\sqrt{-1} = i$ to simplify square roots.

Simplify.

$$\sqrt{-25}$$

$$\sqrt{(25)(-1)}$$

Factor out -1 .

$$\sqrt{(25)} \sqrt{-1}$$

Separate roots.

$$5\sqrt{-1}$$

Simplify.

$$5i$$

Express in terms of i .

$$-\sqrt{-48}$$

$$-\sqrt{(48)(-1)}$$

Factor out -1 .

$$-\sqrt{(48)} \sqrt{-1}$$

Separate roots.

$$-\sqrt{16} \sqrt{3} \sqrt{-1}$$

Factor the perfect square.

$$-4\sqrt{3} \sqrt{-1}$$

Simplify.

$$-4i \sqrt{3}$$

Express in terms of i .



Complex numbers are numbers that can be written in the form $a + bi$.

The **complex conjugate** of $a + bi$ is $a - bi$.

The complex conjugate of $5i$ is $-5i$.

Write as $a + bi$
Find $0 - 5i = -5i$

Express each number in terms of i .

1. $\sqrt{-72}$

2. $4\sqrt{-45}$

3. $\sqrt{-100}$

$$\sqrt{(36)(2)(-1)}$$

$$4\sqrt{(9)(5)(-1)}$$

4. $5\sqrt{-54}$

5. $2\sqrt{-64}$

6. $-\sqrt{-98}$

Find each complex conjugate.

7. $-9i$

8. $1 + 4i$

9. $12 - i$

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Complex Numbers and Roots (continued)

You can use the square root property and $\sqrt{-1} = i$ to solve quadratic equations with imaginary solutions.

Solve $x^2 = -64$.

$$\sqrt{x^2} = \pm\sqrt{-64}$$

Take the square root of both sides.

$$x = \pm 8i$$

Express in terms of i .

Check each root: $(8i)^2 = 64i^2 = 64(-1) = -64$

$$(-8i)^2 = 64i^2 = 64(-1) = -64$$

Remember: $(\sqrt{-1})^2 = i^2 = -1$

Solve $5x^2 + 80 = 0$.

$$5x^2 = -80$$

Subtract 80 from both sides.

$$x^2 = -16$$

Divide both sides by 5.

$$\sqrt{x^2} = \pm\sqrt{-16}$$

Take the square root of both sides.

$$x = \pm 4i$$

Express in terms of i .

Check each root:

$$5(4i)^2 + 80$$

$$5(-4i)^2 + 80$$

$$5(16)i^2 + 80$$

$$5(16)i^2 + 80$$

$$80(-1) + 80$$

$$80(-1) + 80$$

$$0$$

$$0$$

Solve each equation.

10. $x^2 + 18 = 0$

$$x^2 = -18$$

$$x = \pm\sqrt{(9)(2)(-1)}$$

11. $6x^2 + 24 = 0$

$$6x^2 = -24$$

12. $x^2 + 49 = 0$

13. $x^2 + 100 = 0$

14. $3x^2 + 108 = 0$

15. $x^2 + 12 = 0$

13. a. The beginning and end of the flight when the speed of the rocket is 0
 b. $t = -3 \pm 5i$
 c. No; possible answer: the zeros are imaginary because the graph never crosses the x -axis so the function never equals 0. The speed of the rocket must be 0 before takeoff and after landing.

Reteach

1. $6i\sqrt{2}$
2. $12i\sqrt{2}$
3. $10i$
4. $15i\sqrt{6}$
5. $16i$
6. $-7i\sqrt{2}$
7. $9i$
8. $1 - 4i$
9. $12 + i$
10. $x = \pm 3i\sqrt{2}$
11. $x = \pm\sqrt{-4}$
 $x = \pm 2i$
12. $x^2 = -49$
 $x = \pm\sqrt{-49}$
 $x = \pm 7i$
13. $x^2 = -100$
 $x = \pm\sqrt{-100}$
 $x = \pm 10i$
14. $x^2 = -36$
 $x = \pm\sqrt{-36}$
 $x = \pm 6i$
15. $x^2 = -12$
 $x = \pm\sqrt{(4)(3)(-1)}$
 $x = \pm 2i\sqrt{3}$

Challenge

1. $2i, -7i$
2. $-6i, -8i$
3. $9i, -12i$
4. $5i, 49i$
5. $-16i, -36i$
6. $-\frac{4}{3}i, -i$
7. $\frac{1}{5}i, 2i$
8. $-3i, -5i$
9. $-\frac{13}{4}i, 5i$
10. $\frac{5}{6}i, \frac{3}{2}i$

Problem Solving

1. a. $t = 1 \pm \frac{i}{2}$
 b. No; possible answer: the roots are imaginary numbers.
2. a.

b	Function	Roots
24	$d(t) = 16t^2 - 24t + 20$	$\frac{1}{4}(3 \pm i\sqrt{11})$
32	$d(t) = 16t^2 - __t + 20$	$1 \pm \frac{i}{2}$
40	$d(t) = 16t^2 - __t + 20$	$\frac{1}{4}(5 \pm \sqrt{5})$
48	$d(t) = 16t^2 - __t + 20$	$\frac{3}{2} \pm \sqrt{1}$

b. $b = 40$ and 48

c. Possible answer: Real roots mean that ringing the bell is possible.

3. About 36 feet per second
4. C
5. D

Reading Strategies

1. $i\sqrt{9}; 3i; \sqrt{-8}$
2. $3i$ or $-3i$
3. a. $x^2 = -1$, so $x = \pm\sqrt{-1}$, $x = i$ and $-i$
 b. Because the square of a real number cannot be a negative number
4. $(\sqrt{5}i)^2 = (\sqrt{5})^2(i)^2 = 5(-1) = -5$; $(-\sqrt{5}i)^2 = (-\sqrt{5})^2(i)^2 = 5(-1) = -5$
5. Real number; $(3i)(5i) = 15i^2 = 15(-1) = -15$